

Qubit 101

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A Tour of
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The Origins of
Quantum
Computing

Double Slits
and Qubits

ZX to the
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Some Remarks
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Qubit 101: What is Quantum Computing?

Linh Dinh

August 2025



DALHOUSIE
UNIVERSITY

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Most jobs in our modern world rely on computers:

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Most jobs in our modern world rely on computers:

- Finding the best placement for utilities within a city.



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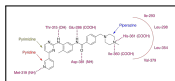
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Most jobs in our modern world rely on computers:

- Finding the best placement for utilities within a city.
- Aiding in the development of new drugs.



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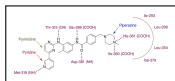
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Most jobs in our modern world rely on computers:

- Finding the best placement for utilities within a city.
- Aiding in the development of new drugs.
- Sending information securely across great distances.

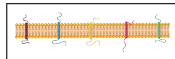
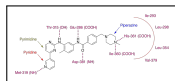


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Most jobs in our modern world rely on computers:

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- Simulating biological processes that are too hard to predict by hand.



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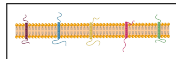
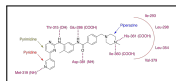
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Most jobs in our modern world rely on computers:

- Finding the best placement for utilities within a city.
- Aiding in the development of new drugs.
- Sending information securely across great distances.
- Simulating biological processes that are too hard to predict by hand.
- As a framework for agent-based modeling in sociology.



Machine Learning Applications:

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Recently, machine learning has become popular for its ability to identify patterns in data. This is more than just ChatGPT!

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- Early identification of tumors in brain scans.



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- Early identification of tumors in brain scans.
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- Finding patterns in large collections of sociological data.
- Analyzing stone artifacts to determine their composition and use.



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- Early identification of tumors in brain scans.
- Finding patterns in large collections of sociological data.
- Analyzing stone artifacts to determine their composition and use.
- Tracking the migratory patterns of wild animals.



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Complex problems and more data to handle



There are limits to what computers can do



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Complex problems and more data to handle



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Solution!

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The Origins of Quantum Computing

The Strange World of Quantum Mechanics

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Nature doesn't follow normal rules:

- Double-Slit Experiments (1800s–1920s):
 - Particles like electrons act like waves.
 - But if you check, they act like particles!



The Strange World of Quantum Mechanics

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- Photoelectric Effect (1905):

- Albert Einstein showed light acts like particles (photons), not just waves.



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- Photoelectric Effect (1905):

- Albert Einstein showed light acts like particles (photons), not just waves.



- Bohr's Atomic Model (1913):

- Niels Bohr said electrons jump between specific energy levels in atoms, like steps on a ladder, not smoothly.



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- It was very confusing for all the physicists involved.



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- It was very confusing for all the physicists involved.



- Einstein was reluctant to even accept some of the conclusions of quantum mechanics, which we now know to be true!

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- Einstein was reluctant to even accept some of the conclusions of quantum mechanics, which we now know to be true!

Einstein and Entanglement

You will learn more about this story in the afternoon.

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- **1920s – 1930s:** Scientists such as Paul Dirac and Werner Heisenberg developed the math rules to understand the puzzling world of quantum mechanics.



(a) Paul Dirac



(b) Werner Heisenberg

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- **1930s – 1980s:** Playing by these rules, scientists were able to predict many phenomena, such as how chemicals interact.

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(a) Paul Dirac



(b) Werner Heisenberg

- **1930s – 1980s:** Playing by these rules, scientists were able to predict many phenomena, such as how chemicals interact.

However...

The rules were too tedious to work with by hand... They were even too tedious for computers!

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(a) Paul Dirac



(b) Werner Heisenberg

- **1930s – 1980s:** Playing by these rules, scientists were able to predict many phenomena, such as how chemicals interact.
- **1981:** Richard Feynman suggested building computers with quantum particles, since the particles already play by these rules.



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(1981) Surely you're joking, Mr. Feynman!

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(1981) Surely you're joking, Mr. Feynman!



(1983) Quantum computers could secure your emails?

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(1983) Quantum computers could secure your emails?



(1997) Quantum computers could expose your emails!?



(2001) A real quantum computer by IBM and Stanford!

Applications of Quantum Computing

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So what can quantum computers do?

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So what can quantum computers do?

- Quantum computers offer exciting new solutions to all of the problems mentioned at the beginning of this lesson!

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So what can quantum computers do?

- Quantum computers offer exciting new solutions to all of the problems mentioned at the beginning of this lesson!
- Recently, quantum machine learning has been gaining attention. The goal is to overcome the challenges of machine learning through the principles of quantum mechanics!

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So what can quantum computers do?

- Quantum computers offer exciting new solutions to all of the problems mentioned at the beginning of this lesson!
- Recently, quantum machine learning has been gaining attention. The goal is to overcome the challenges of machine learning through the principles of quantum mechanics!

More Quantum Hype?

Is quantum machine learning the next big thing, or simply more quantum hype? Only time will tell!

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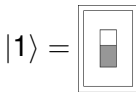
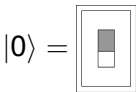
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- You have probably heard that computers store data using bits. These are like light switches, you can turn them on or off. We will call on $|1\rangle$ and off $|0\rangle$.



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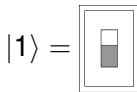
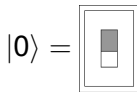
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- If a light switch is set to $|1\rangle$, then it is *true* that the light is turned on. For this reason, we often think of $|0\rangle$ as saying something is **false**, and $|1\rangle$ as saying something is **true**.

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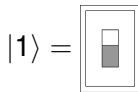
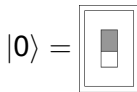
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Question Time!

What could we keep track of using a single bit? How about two bits?

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Playing with Switches

Light switches are meant to be used! Can anyone think of an operation that we can apply to a light switch?

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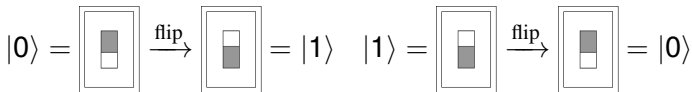
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- If we have a light switch, we can flip it! We can think of this as turning **false** into **true** and **true** into **false**. If something is **not true** then it is false, so we call this a NOT gate!



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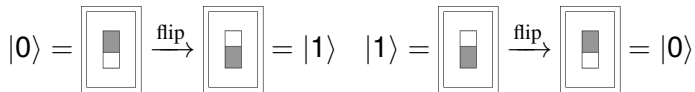
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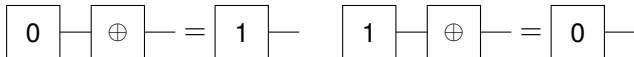
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- We will typically write the NOT gate using the \oplus symbol. Using this we can turn math into pictures!



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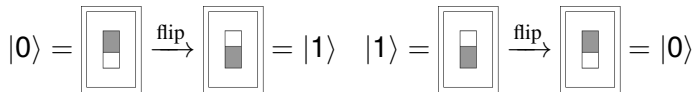
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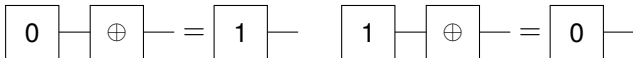
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- If we have a light switch, we can flip it! We can think of this as turning **false** into **true** and **true** into **false**. If something is **not true** then it is false, so we call this a NOT gate!



- We will typically write the NOT gate using the \oplus symbol. Using this we can turn math into pictures!



Exercise Time!

Do you think that $\text{---} \oplus \text{---} \oplus \text{---}$ is the same as --- ?

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
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Now to the exciting part: what is a qubit?

- If you have ever played with a light switch before, then you surely know that it can get stuck between on and off. For a conventional bit, this would be a bug!


$$= |?! \rangle$$

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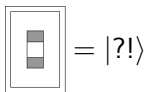
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$$\boxed{\begin{array}{c} \text{grey} \\ \text{white} \\ \text{grey} \end{array}} = |?! \rangle$$

- Quantum computing replaces bits with *qubits* made from quantum particles. This isn't science fiction, it's real!

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
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$$= |?! \rangle$$

- Quantum computing replaces bits with *qubits* made from quantum particles. This isn't science fiction, it's real!
- A qubit can be anywhere between $|0\rangle$ and $|1\rangle$, though this is better thought of as being partly $|0\rangle$ and $|1\rangle$ at the same time. We call this *quantum superposition*!

Double Slits Experiment

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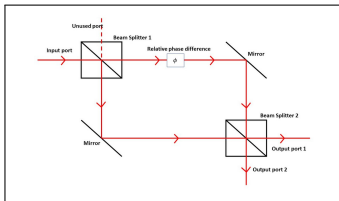
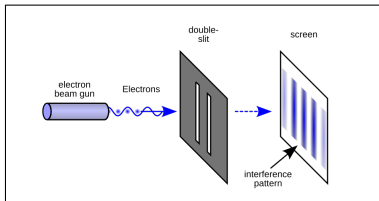
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The electrons in the double slit experiment are qubits.

- The qubit is in state $|0\rangle$ if it goes through the first slit.
- The qubit is in state $|1\rangle$ if it goes through the second slit.
- The qubit is in superposition when it acts like a wave.

Double Slits and Qubits

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The electrons in the double slit experiment are qubits.

- The qubit is in state $|0\rangle$ if it goes through the first slit.
- The qubit is in state $|1\rangle$ if it goes through the second slit.
- The qubit is in superposition when it acts like a wave.

A Quantum NOT Gate?

What would it mean to apply a NOT gate to the electron in the double slit experiment? Does our light switch analogy work anymore?

Double Slits and Qubits

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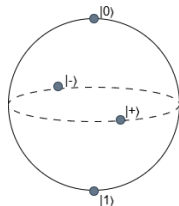
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Experiments have shown that qubits have many ways to be between $|0\rangle$ and $|1\rangle$. We can visualize these superpositions as points on a ball (the Bloch sphere).



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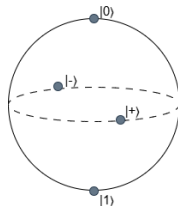
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The NOT Gate Revisited

Is there a way to do the NOT gate without moving $|+\rangle$ and $|-\rangle$?
What sort of rotation would this be?

Spinning the Bloch Sphere

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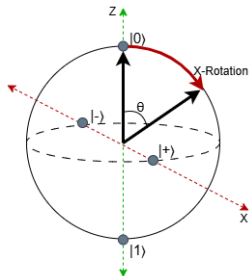
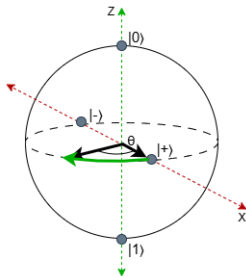
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In quantum computing, we care about two special kinds of rotations: the Z -rotations and the X -rotations.



Spinning the Bloch Sphere

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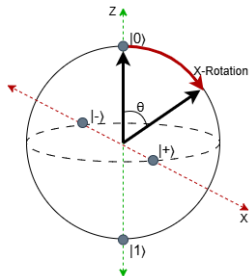
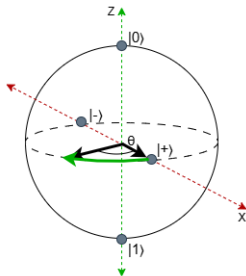
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In quantum computing, we care about two special kinds of rotations: the Z -rotations and the X -rotations.



Is This Enough?

Using only the Z -rotations and the X -rotations, is it possible to rotate the Bloch sphere in every possible way?

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ZX-Calculus: Background

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If we would like to jump into the world of quantum computing, we will need to know the rules of the game. Unfortunately, the rules developed in the early 1900s are very tedious...

$$(\sigma_Z \otimes I) \circ (I \oplus \sigma_X) \circ (\sigma_X \oplus I) \circ (I \oplus \sigma_X) \circ (I \otimes \sigma_Z) = \text{SWAP}$$

ZX-Calculus: Background

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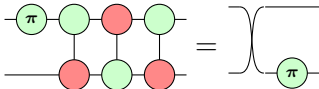
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Thankfully, there is an easier way to do this! The ZX-calculus, developed by Bob Coecke and Ross Duncan in 2008, provides us with a graphical language for these complicated equations!



ZX-Calculus: Background

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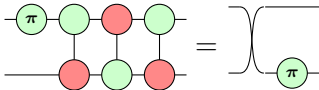
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Let's spend some time learning what this tells us about qubit states.

ZX-Calculus: Qubit States

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In the ZX-calculus, we associate the colour green with Z -rotations and the colour red with X -rotations.

ZX-Calculus: Qubit States

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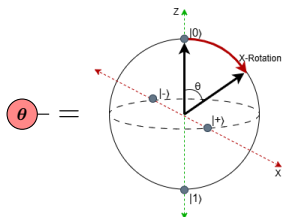
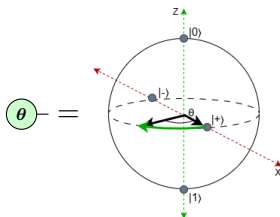
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In the ZX-calculus, we associate the colour green with Z -rotations and the colour red with X -rotations.

Green dots let us rotate $|+\rangle$ around the X -axis and red dots let us rotate $|0\rangle$ around the X -axis.



ZX-Calculus: Qubit States

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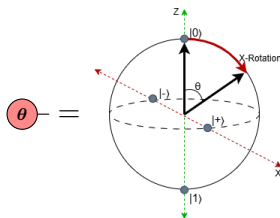
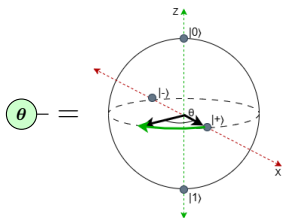
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Green dots let us rotate $|+\rangle$ around the X -axis and red dots let us rotate $|0\rangle$ around the X -axis.



Check Your Understanding

What are π (in a green circle) and π (in a red circle)? What are 2π (in a green circle) and 2π (in a red circle)?

ZX-Calculus: Learning the Rules

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What if we want to take a qubit and rotate it? We write the rotations like $-\textcircled{\theta}-$ and $-\textcircled{\theta}-$. To rotate the state, we simply join the two dots together!

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$\text{---}(\pi)\text{---}(\frac{\pi}{3})\text{---}$ rotates $|1\rangle$ by $(\pi/3)$ -radians about the Z -axis.

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So what are the rules for a single qubit?

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$$\text{---}(0)\text{---} = |+\rangle = \text{---}(\text{green})\text{---}$$

$$\text{---}(0)\text{---} = |0\rangle = \text{---}(\text{red})\text{---}$$

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$$\text{---}(0)\text{---} = |0\rangle = \text{---}(\text{red})\text{---}$$

$$\text{---}(\pi)\text{---} = |1\rangle$$

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$$\text{---}(0)\text{---} = |0\rangle = \text{---}(\text{red})\text{---}$$

$$\text{---}(\pi)\text{---} = |1\rangle$$

$$\text{---}(\theta)\text{---} = \text{---}(\text{red})\text{---}(\theta)\text{---}$$

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$$\begin{aligned} \text{---}(0)\text{---} &= |0\rangle = \text{---}(\text{red})\text{---} \\ \text{---}(\pi)\text{---} &= |1\rangle \\ \text{---}(\theta)\text{---} &= \text{---}(\text{red})\text{---}(\theta)\text{---} \\ \text{---}(\text{red})\text{---} &= \text{---} = \text{---}(2\pi)\text{---} \end{aligned}$$

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$$\begin{aligned} \text{---}(0)\text{---} &= |0\rangle = \text{---}(\text{red})\text{---} \\ \text{---}(\pi)\text{---} &= |1\rangle \\ \text{---}(\theta)\text{---} &= \text{---}(\text{red})\text{---}(\theta)\text{---} \\ \text{---}(\text{red})\text{---} &= \text{---} = \text{---}(2\pi)\text{---} \\ \text{---}(\alpha)(\beta)\text{---} &= \text{---}(\alpha+\beta)\text{---} \end{aligned}$$

Example: A Rotation Chain

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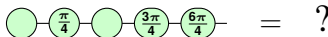
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$$\text{---} \bigcirc \text{---} \bigcirc \frac{\pi}{4} \text{---} \bigcirc \text{---} \bigcirc \frac{3\pi}{4} \text{---} \bigcirc \frac{6\pi}{4} \text{---} = ?$$

Example: A Rotation Chain

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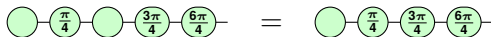
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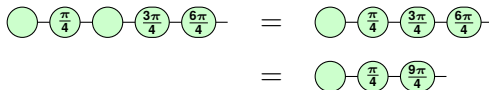
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$$\begin{aligned} & \text{---} \bigcirc \text{---} \bigcirc \frac{\pi}{4} \text{---} \bigcirc \text{---} \bigcirc \frac{3\pi}{4} \text{---} \bigcirc \frac{6\pi}{4} \text{---} &= & \text{---} \bigcirc \text{---} \bigcirc \frac{\pi}{4} \text{---} \bigcirc \frac{3\pi}{4} \text{---} \bigcirc \frac{6\pi}{4} \text{---} \\ & &= & \text{---} \bigcirc \text{---} \bigcirc \frac{\pi}{4} \text{---} \bigcirc \frac{9\pi}{4} \text{---} \\ & &= & \text{---} \bigcirc \text{---} \bigcirc \frac{10\pi}{4} \text{---} \end{aligned}$$

Example: A Rotation Chain

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$$\begin{aligned} & \text{---} \bigcirc \text{---} \bigcirc \frac{\pi}{4} \text{---} \bigcirc \text{---} \bigcirc \frac{3\pi}{4} \text{---} \bigcirc \frac{6\pi}{4} \text{---} &= & \text{---} \bigcirc \text{---} \bigcirc \frac{\pi}{4} \text{---} \bigcirc \frac{3\pi}{4} \text{---} \bigcirc \frac{6\pi}{4} \text{---} \\ & &= & \text{---} \bigcirc \text{---} \bigcirc \frac{\pi}{4} \text{---} \bigcirc \frac{9\pi}{4} \text{---} \\ & &= & \text{---} \bigcirc \text{---} \bigcirc \frac{10\pi}{4} \text{---} \\ & &= & \text{---} \bigcirc \frac{10\pi}{4} \text{---} \end{aligned}$$

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Are We Done Yet?

We should be careful. What happens if we rotate the Bloch sphere by $2\pi = 8\pi/4$ radians?

Example: A Rotation Chain

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Example: A Rotation Chain

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$$\begin{aligned}
 & \text{---} \bigcirc \text{---} \bigcirc \frac{\pi}{4} \text{---} \bigcirc \text{---} \bigcirc \frac{3\pi}{4} \text{---} \bigcirc \frac{6\pi}{4} \text{---} &= & \text{---} \bigcirc \text{---} \bigcirc \frac{\pi}{4} \text{---} \bigcirc \frac{3\pi}{4} \text{---} \bigcirc \frac{6\pi}{4} \text{---} \\
 & &= & \text{---} \bigcirc \text{---} \bigcirc \frac{\pi}{4} \text{---} \bigcirc \frac{9\pi}{4} \text{---} \\
 & &= & \text{---} \bigcirc \text{---} \bigcirc \frac{10\pi}{4} \text{---} \\
 & &= & \text{---} \bigcirc \frac{10\pi}{4} \text{---} \\
 & &= & \text{---} \bigcirc \frac{\pi}{2} \text{---} \bigcirc 2\pi \text{---} \\
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 & &= & \text{---} |-\rangle
 \end{aligned}$$

Preparing a Superposition State

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States that fall half-way between $|0\rangle$ and $|1\rangle$ on the Bloch sphere, such as $|+\rangle$ and $|-\rangle$, are very important in quantum computing. However, we usually start with all of our qubits in the state $|0\rangle$.

Preparing a Superposition State

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A New Gate?

Is it possible to switch $|0\rangle$ with $|+\rangle$ and $|1\rangle$ with $|-\rangle$. This would give us easy access to both superpositions.

Preparing a Superposition State

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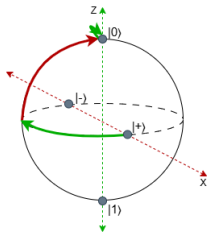
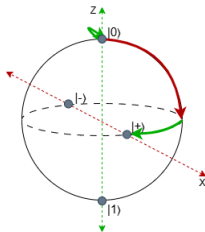
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A New Gate?

Is it possible to switch $|0\rangle$ with $|+\rangle$ and $|1\rangle$ with $|-\rangle$. This would give us easy access to both superpositions.

This turns out to be tricky, but possible!



The Hadamard Gate

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We call this new rotation the *Hadamard gate*. Since it swaps $|0\rangle$ with $|+\rangle$ and $|1\rangle$ with $|-\rangle$, then applying two Hadamard gates to the Bloch sphere sends us back to where we started.



The Hadamard Gate

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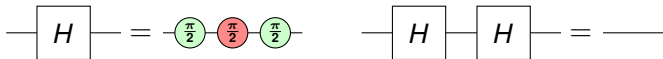
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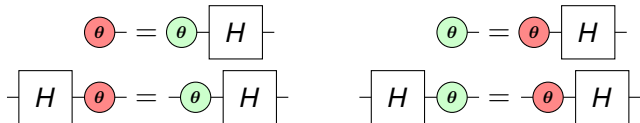
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Intuitively, the Hadamard gate lets us swap the colours of dots.



Oh no! NOT Again!

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Remember for earlier in this lecture that the controlled NOT gate is the same as the $-\pi$ rotation.

Oh no! NOT Again!

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Remember for earlier in this lecture that the controlled NOT gate is the same as the $-\pi$ rotation.

Not a Superposition?

What would the NOT gate do to $-\theta$?

Oh no! NOT Again!

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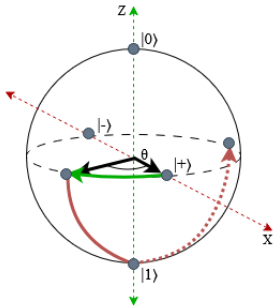
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Remember for earlier in this lecture that the controlled NOT gate is the same as the $-\pi$ rotation.

To understand how Z -rotations and X -rotations interact, it might help to look at what happens on the Bloch sphere.



Oh no! NOT Again!

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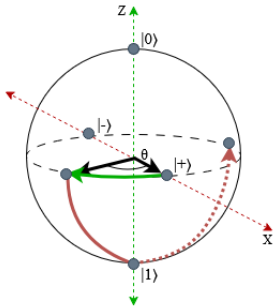
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To understand how Z -rotations and X -rotations interact, it might help to look at what happens on the Bloch sphere.



Playing with the Bloch sphere, we can confirm that $-\theta$ π is the same as $-\pi$ $-\theta$. You can try this on your own over one of the breaks.

Example: A Hadamard Colour Change

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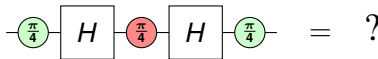
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Example: A Hadamard Colour Change

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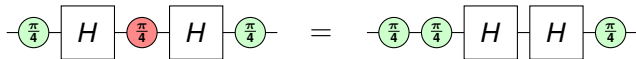
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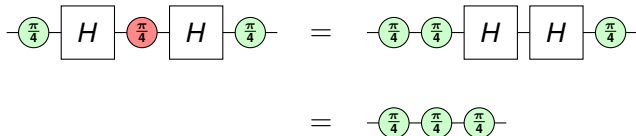
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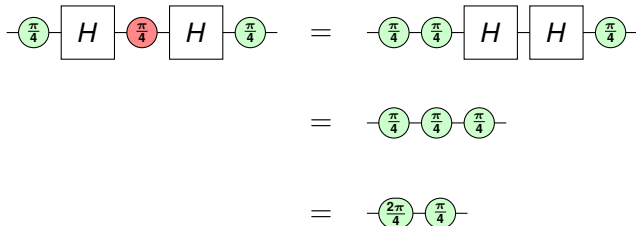
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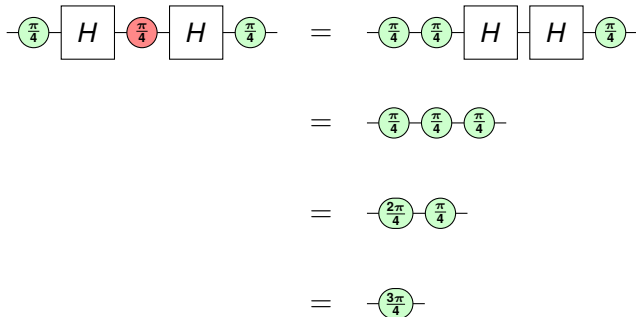
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Single Quantum Gates

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In quantum circuits, we write X - and Z -rotations as gates:

$$\boxed{R_X(\theta)} = \text{red circle with } \theta$$

$$\boxed{R_Z(\theta)} = \text{green circle with } \theta$$

Single Quantum Gates

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In quantum circuits, we write X - and Z -rotations as gates:

$$\boxed{R_X(\theta)} = \text{red circle with } \theta$$

$$\boxed{R_Z(\theta)} = \text{green circle with } \theta$$

We also give special gate names to commonly used rotations:

$$\boxed{X} = \text{red circle with } \pi$$

$$\boxed{Z} = \text{green circle with } \pi$$

$$\boxed{H} = \text{green circle with } \frac{\pi}{2}, \text{ red circle with } \frac{\pi}{2}, \text{ green circle with } \frac{\pi}{2}$$

$$\boxed{X^{1/2}} = \text{red circle with } \frac{\pi}{2}$$

$$\boxed{S} = \text{green circle with } \frac{\pi}{2}$$

$$\boxed{T} = \text{green circle with } \frac{\pi}{4}$$

$$\boxed{X^{-1/2}} = \text{red circle with } -\frac{\pi}{2}$$

$$\boxed{S^{-1}} = \text{green circle with } -\frac{\pi}{2}$$

$$\boxed{T^{-1}} = \text{green circle with } -\frac{\pi}{4}$$

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Rotating the Poles

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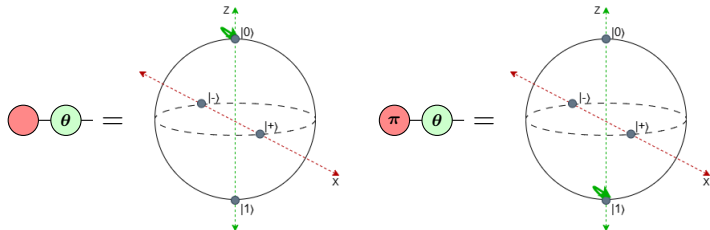
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We can think of $|0\rangle$ and $|1\rangle$ as the north and south poles of the Bloch sphere. If we rotate the Bloch sphere along the Z -axis, then neither pole should move.



Rotating the Poles

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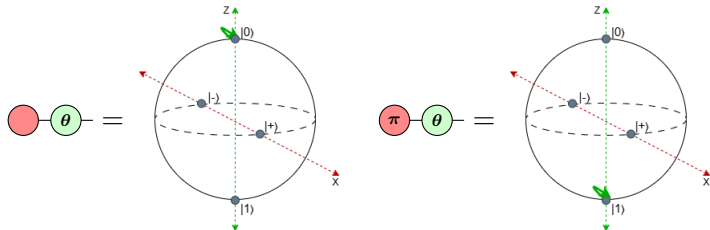
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We can think of $|0\rangle$ and $|1\rangle$ as the north and south poles of the Bloch sphere. If we rotate the Bloch sphere along the Z -axis, then neither pole should move.



If we were not using the ZX-calculus, then some of the other math tools might tell us that $\pi - \theta$ actually isn't $|1\rangle$. However, many experiments have shown that this change is *undetectable*.

A Warning About Global Phase

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These undetectable changes are called *global phase*. We might come across this while working with quantum software...

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These undetectable changes are called *global phase*. We might come across this while working with quantum software...

In this workshop, we will be working with Quirk. This program will visualize qubits on the Bloch sphere and show us the amplitude of each state (more on this later).



A Warning About Global Phase

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In this workshop, we will be working with Quirk. This program will visualize qubits on the Bloch sphere and show us the amplitude of each state (more on this later).



If we apply a Z -rotation to the qubit in state $|1\rangle$, then the amplitude will seemingly change, as a result of global phase!



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